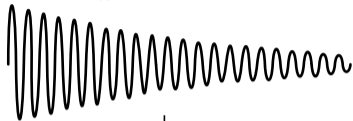
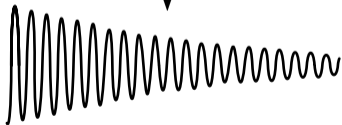


$$h(t) = Ae^{-\sigma t} \sin \omega_d t$$

a)

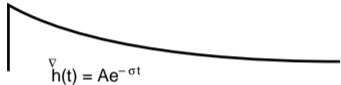


b)



$$\tilde{h}(t) = Ae^{-\sigma t} \cos \omega_d t$$

c)



$$\overset{\nabla}{h}(t) = h(t) + i\tilde{h}(t)$$

$$|\overset{\nabla}{h}(t)| = \sqrt{h^2(t) + \tilde{h}^2(t)}$$

the resonance peak. $B_{3dB} = 2\sigma$. In this case B_{3dB} is of the order of the resolution; consequently a determination of the B_{3dB} (and hence σ) will be very inaccurate. Two methods can be used to obtain a more accurate estimate of the damping:

1. A (time consuming) zoom analysis using a much smaller Δf . This involves a new analysis for each resonance, making five new measurements in total.
2. The damping at each resonance can be determined from the envelope of the associated impulse response function. This method is illustrated in Figs. 2 to 7, from which σ (decay constant) for each resonance can be easily found from the original measurement.

Fig. 2 shows the frequency response function, and Fig. 3 shows the corresponding impulse response function. However, this cannot be used to calculate σ , as it contains five exponentially damped sinusoids (one for each resonance) superimposed.

Fig. 4 shows a single resonance which has been isolated using the frequency weighting facility of Type 3550. The corresponding impulse response function, shown in Fig. 5, clearly shows the exponential decaying sinusoid.

Fig. 6 shows the magnitude of the analytic signal of the impulse response function on a linear amplitude scale. By using a log. amplitude axis, the envelope is a straight line, see Fig. 7. The analyzer's reference cursor is used to measure the time constant τ corresponding to an amplitude decay of 8.7 dB. From τ , the decay constant and hence the damping of the resonance can be calculated directly ($\sigma = 1/\tau$).

By using the Hilbert transform, it is possible to determine the decay constant for the five individual resonances, without having to make new, more narrow banded measurements. This method applies to the 3550 family. The 2140 family does not support frequency weighting.

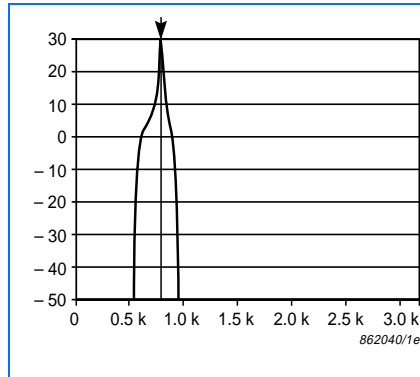


Fig 4

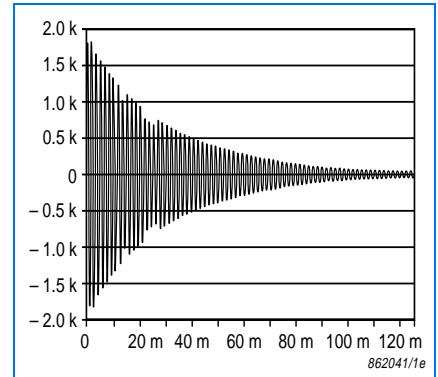


Fig 5

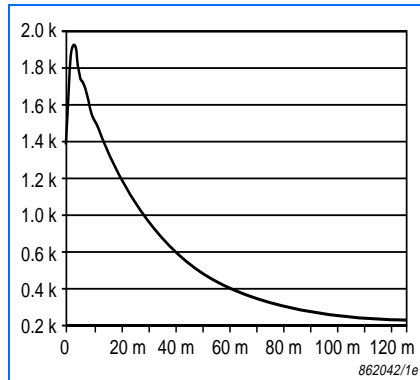


Fig 6

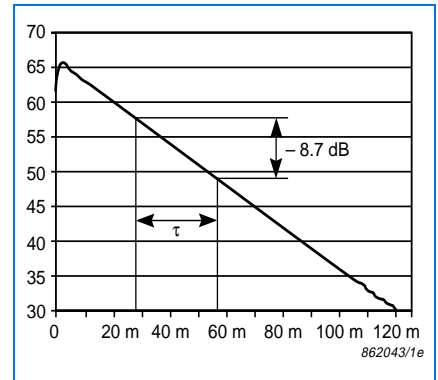


Fig 7

Propagation time estimation

The propagation time (from point A to B) of a signal is usually estimated by measuring the signal at A and B, and calculating the cross correlation function $R_{AB}(t)$.

By using the Hilbert transform, the correct propagation time can easily be found from the envelope of the cross correlation function, see Fig. 8, whether or not the peak of $R_{AB}(t)$ corresponds to the envelope maximum.

References

A short discussion of the Hilbert transform can be found in ref. [1], while ref. [2] discusses the properties and applications of the Hilbert transform. Ref. [3] gives additional information about damping measurement in general.

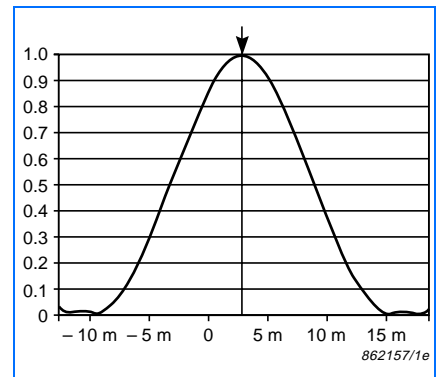


Fig 8

- [1]. N. Thrane: "The Hilbert Transform", Technical Review No. 3 1984, Brüel & Kjær, BV 0015
- [2]. J.S. Bendat: "The Hilbert Transform and Applications to Correlation Measurements", Brüel & Kjær, 1985, BT0008
- [3]. S.Gade, H.Herlufsen: "Digital Filter Techniques vs. FFT Techniques for Damping Measurements", Technical Review No. 1 1994, Brüel & Kjær, BV 0044